

$$(10) \Delta U_i = i_i \frac{\partial U_i}{\partial A_i} \Delta C_i + \frac{\partial U_i}{\partial A_i} i_i \Delta S_i, \text{ or}$$

$$(11) \Delta U_i = i_i \frac{\partial U_i}{\partial A_i} \Delta Y_i.$$

We define a Social Welfare Function for all the individuals i in the economy.

$$(12) W = \sum_i U_i.$$

Then

$$(13) \Delta W_c = \sum_i \frac{\partial U_i}{\partial A_i} i_i \Delta Y_i, \text{ where } c \text{ refers to costs.}$$

We assume that $\frac{\partial U_i}{\partial A_i}$ is the same for all individuals and equal to the arbitrary constant α . Then

$$(14) \Delta W_c = \alpha \sum_i i_i \Delta Y_i.$$

ΔW_c measures the costs in the analysis. The benefits are a flow of future annual income accruing to various individuals, or

$$(15) B = \sum_i \Delta B_i.$$

Assuming the value of marginal future income the same for beneficiaries as for taxpayers, we have

$$(16) \Delta W_b = \alpha \sum_i \Delta B_i.$$

In order for a project to represent a favorable economic change, the value of benefits must exceed the value of costs, or $\Delta W_b > \Delta W_c$. This requires

$$(17) \alpha \sum_i \Delta B_i > \alpha \sum_i i_i \Delta Y_i.$$

This inequality is unaffected by the value for α . For convenience, let $\alpha = 1$. Then the criterion becomes

$$(18) \sum_i \Delta B_i > \sum_i i_i \Delta Y_i \text{ or}$$

$$(19) \frac{\sum_i \Delta B_i}{\sum_i i_i \Delta Y_i} > 1.$$

Use of the interest rate that our analysis seeks to estimate for benefit-cost analysis is equivalent to criterion (19). We have esti-